

You can ELIMINATE if and only if:

1) _____

2) _____

Example 1:

$$1) \begin{cases} 3x - y = 8 \\ 2x + y = 7 \end{cases}$$

$$2) \begin{cases} x + y = 14 \\ x - y = 4 \end{cases}$$

$$3) \begin{cases} 3x + 2y = 7 \\ 5x - 2y = 1 \end{cases}$$

$$1) \begin{cases} 4x + 5y = 6 \\ 4x - 2y = -8 \end{cases}$$

$$2) \begin{cases} 3x + 2y = 2 \\ -1(3x + y) = (7) - 1 \end{cases}$$

$$\begin{array}{r} 3x + 2y = 2 \\ -3x - y = -7 \\ \hline y = -5 \end{array}$$

$$3x + 2(-5) = 2$$

$$3x - 10 = 2$$

$$3x = 12$$

$$x = 4$$

~~X~~
Consistent
Independent

$$3) \begin{cases} x - 2y = 2 \\ 3x = 2y + 10 \\ -2y - 2y \end{cases}$$

$$\begin{array}{r} 4 - 2y = 2 \\ -4 \quad -4 \\ \hline -2y = -2 \\ y = 1 \end{array}$$

$$\begin{array}{r} (4, 1) \\ x - 2y = 2 \\ -1(3x - 2y) = -10 \end{array}$$

$$\begin{array}{r} x - 2y = 2 \\ -3x + 2y = -10 \\ \hline -2x = -8 \\ x = 4 \end{array}$$

$$\begin{array}{r} 12 = 2y + 10 \\ 2 = 2y \\ 1 : y \end{array}$$

$$4) \begin{cases} 2x + y = 25 \\ 2x = 5y + 7 \end{cases}$$

Independent Systems:

$$1) \begin{cases} 2x + 5y = 15 \\ -4x + 7y = -13 \end{cases}$$

$$2x + 5(1) = 15$$

$$2x + 5 = 15$$

$$2x = 10$$

$$x = 5$$

$$(5, 1)$$

$$4x + 10y = 30$$

$$-4x + 7y = -13$$

$$\hline 17y = 17$$

$$y = 1$$

I.C. (C.I.)

$$2) \begin{cases} 6r + 7t = -15 \\ 2(-3r + t) = (-6) \cdot 2 \end{cases}$$

$$\begin{array}{r} 6r + 7t = -15 \\ -6r + 2t = -12 \\ \hline \end{array}$$

$$6r + 7(-3) = -15$$

$$\begin{array}{r} 6r - 21 = -15 \\ +21 \quad +21 \\ \hline \end{array}$$

$$6r = 6$$

$$r = 1$$

$$9t = -27$$

$$t = -3$$

$$(1, -3)$$

Consistent
Indep

$$\begin{array}{l} -5(2x - 7y = 3) -5 \\ 3) \quad 2(5x - 4y = -6) 2 \end{array}$$

$$\begin{array}{r} (-2, -1) \\ -10x + 35y = -15 \\ 10x - 8y = -12 \\ \hline \end{array}$$

$$2x - 7(-1) = 3$$

$$\begin{array}{r} 2x + 7 = 3 \\ -7 \quad -7 \\ \hline 2x = -4 \\ x = -2 \end{array}$$

$$27y = -27$$

$$y = -1$$

Consistent
Ind.

$$4) \begin{cases} 2y - 4x = 18 \\ -5x + 3y = 23 \end{cases}$$

Dependent and Inconsistent Systems:

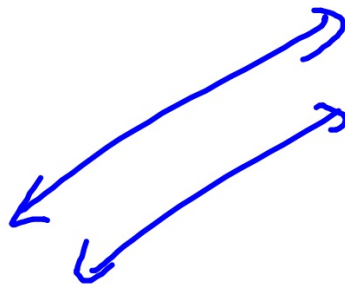
$$5) \begin{cases} 2x + 5y = 12 \\ 2x + 5y = 15 \end{cases}$$

$$\begin{array}{r} -2x - 5y = -12 \\ 2x + 5y = 15 \\ \hline \end{array}$$

$$0 = 3$$

No Solution

Inconsistent



$$6) \begin{cases} 8x + 4y = -16 \\ 2x + y = -4 \end{cases}$$

1)
$$\begin{cases} 5x + 3y = 2 \\ 2x + 20 = 4y \end{cases}$$

$$2) \begin{cases} 2x = 5 + 4y \\ 2y = 8 + x \end{cases}$$

$$3) \begin{cases} 4y + 30 = 10x \\ 5x - 2y = 15 \end{cases}$$